# THE MILLIMETER-WAVE PROPERTIES OF SUPERCONDUCTING MICROSTRIP LINES

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### **ABSTRACT**

We have developed a novel technique for making high quality measurements of the millimeter-wave properties of superconducting thin-film microstrip transmission lines. Our experimental technique currently covers the 75–130 GHz frequency range. The method is based on standing wave resonances in an open ended transmission line. We obtain information on the characteristic impedance, phase velocity, and loss of the microstrip. Our data for Nb/SiO/Nb lines, taken at 4.2 K and 1.6 K, can be explained by a single set of physical parameters, with a temperature-independent loss tangent of tan  $\delta_{SiO} = 1.2 \pm 0.3 \times 10^{-3}$  for our latest samples. The amplitude 1/e attenuation length is 30 cm to 40 cm.

## **INTRODUCTION**

Superconducting microstrip lines are of major importance for tuning elements in SIS mixers<sup>1</sup>. Microstrip lines have also been proposed for use in millimeter and submillimeter direct detection applications, such as antenna coupled bolometer arrays with on-chip band-pass filters<sup>2,3</sup>. Such highly integrated architectures would allow for a very large number of pixels and would enable novel instruments, such as a multiband imaging polarimeter or an on-chip spectrometer. The transmission losses of superconducting microstrip lines are a key issue for the feasibility of such architectures. The properties of superconducting microstrip lines have been investigated previously<sup>4,5</sup>. However, the method that we present here provides much higher quality data.

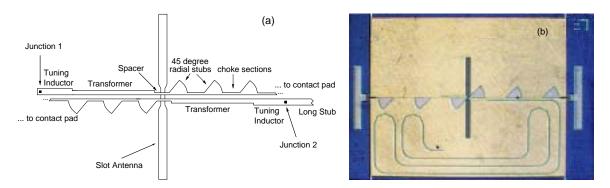
# **EXPERIMENTAL METHOD**

Our method is based on standing wave resonances in an open ended microstrip stub. The entire circuit is fabricated on a thick silicon substrate ( $400\mu m$ ), and the millimeter-wave radiation is coupled onto the chip quasi-optically using a silicon substrate lens<sup>1</sup>. There are two Nb/Al-oxide/Nb SIS junctions on the chip which serve as direct detectors. One of the junctions is connected to an open-ended Nb/SiO/Nb microstrip stub (Figure 1). Having two SIS junctions on the chip allows us to calibrate out changes in the power that is coupled onto the chip from the external signal source. The ratio of the signal from the junction connected to the stub, to the signal from the "power reference" junction, gives us a precise relative power response, whose frequency dependence carries information about the properties of the microstrip stub.

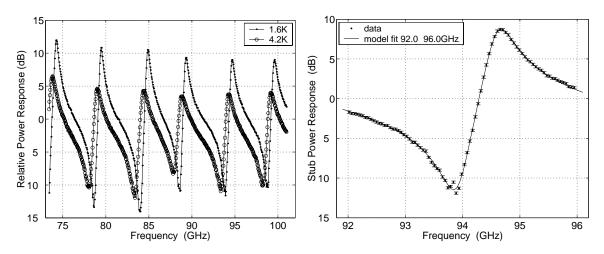
We use two harmonic generators as radiation sources. These harmonic generators are driven by two microwave signal generators (10–18 GHz), and produce a series of coherent millimeter wave frequencies

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that are exact integer multiples of the input signal frequencies. The two microwave signals differ in frequency by a small value (typically 10 MHz), and this difference is multiplied with harmonic number. The two SIS junctions mix these signals and convert the millimeter waves to signals at various RF beat frequencies. By detecting the output signals from the junctions, that are locked to a specific beat frequency, we select out a unique harmonic number and therefore measure the microstrip response at the corresponding frequency. Figure 2(a) shows representative data taken at two different temperatures.



**Figure 1:** (a) Schematic diagram of chip. (b) Photograph of a chip with a 1 cm long microstrip stub. The top strip of the microstrip is 5  $\mu$ m wide, and the thicknesses of the Nb top strip and ground plane layers are 2500 Å each. The thickness of the SiO dielectric is 4000 Å.



**Figure 2:** (a) Microstrip power response vs. frequency at two different temperatures and 2.00mV bias voltage. The loss decreases and the phase velocity increases at the lower temperature, in agreement with theoretical expectations. (b) Example fit of 2.00 mV bias data, at 4.2 K.

### Theoretical model

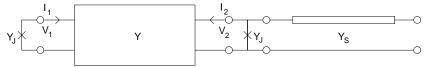


Figure 3: Theoretical model schematic diagram.

We treat the symmetric part of the circuit as a two-port black box linear circuit with unknown admittance matrix Y, which includes the antenna, the junction capacitance, and the matching circuits (Figure 3). The admittance matrix Y does not include the admittance of the junction due to the tunneling currents,  $Y_J$ , or the

microstrip stub. The relative power response is given by the detected power ratio of the two junctions which can be shown to be:

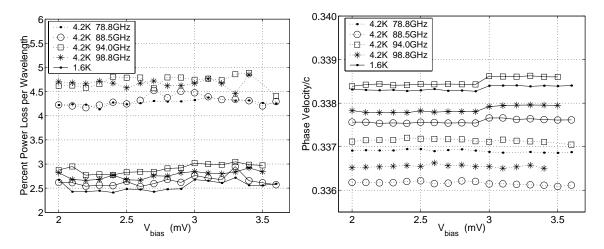
$$P_{dB}(v;K,\tau,w) = 10\log_{10}\left|\frac{V_2}{V_1}\right|^2 = -20\log_{10}\left|1 + w\frac{1 - \tau\exp(-i2Kv)}{1 + \tau\exp(-i2Kv)}\right|. \tag{1}$$

 $K=2\pi L/c$  is the phase constant, where L is the length of the microstrip stub, and c is the phase velocity of the line.  $\tau=\exp(-2\alpha L)$  is the round trip amplitude attenuation, and w is a complex coefficient which depends on the admittances of the circuit elements. We assume that these quantities are essentially constant over the narrow (4 GHz) frequency range of a single resonance, and obtain their values using a least-squares fit to the data. Figure 2(b) shows an example fit of (1) over a 4 GHz frequency range.

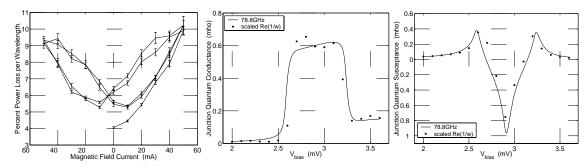
## **RESULTS**

We have taken data in the 75–130 GHz band, at 4.2K and 1.6K, for a wide range of junction bias voltages both below and above the gap voltage. Figure 4(a) shows the measured loss at the two temperatures (for four frequency bins). Although the junction impedance varies greatly from 2.0 mV to 3.6 mV (Figures 5(b),(c)), the extracted values of the loss are essentially independent of bias voltage. This demonstrates that, given the quality of our data, our data analysis technique can reliably separate out the effects of microstrip loss. The difference of about 1.5% power loss per wavelength between the two temperatures is accounted for by the theoretical (Mattis-Bardeen) loss difference in the superconductor. The remaining loss is attributed to the dielectric, with a temperature-independent loss tangent  $\tan \delta_{SiO} = 5.5 \pm 0.3 \times 10^{-3}$ . Figure 4(b) shows the measured phase velocity at the two temperatures.

For our latest devices the fabrication conditions for the SiO were improved (a vacuum leak was fixed), and the loss has dropped by a factor of about five. Now the power loss per wavelength at 1.6K is 0.5%, and the corresponding dielectric loss tangent is  $\tan \delta_{\text{SiO}} = 1.2 \pm 0.3 \times 10^{-3}$ .



**Figure 4:** Experimental results at 4.2 K and 1.6 K, for four frequency values. (a) Percent power loss per wavelength vs. junction bias voltage. (b) Phase velocity vs. junction bias voltage.



**Figure 5:** (a) Power loss per wavelength vs. magnetic field current. The junctions are biased at 2.50 mV, and the first point is taken with the magnetic field turned off. Subsequent points were taken with magnetic field current stepped by 10 mA, ranging between -50 mA, and +50 mA. (b,c) see text.

We have also observed a hysteretic behavior of the loss as a function of the magnetic field strength. In Figure 5(a), the loss vs. magnetic field current (which is proportional to the magnetic field) is shown. We attribute this loss and the "memory" effect (hysteresis) to the creation of fluxons in the superconducting films.

Figures 5(b),(c) show the quantum conductance (susceptance) of the junctions vs. bias voltage<sup>6,7</sup>. The solid lines are calculated from the DC I-V curve. The data points are the real (imaginary) parts of 1/w, which scales as the admittance of the junction  $Y_J$ . The scaling factor yields the characteristic impedance of the microstrip, which we measure to be  $Z_0 = 12.7 \pm 1.6 \ \Omega$ .

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